Elastic and Inelastic Collisions: Air Track

Objectives

In this experiment you will investigate collisions that are (nearly) elastic and others that are completely inelastic. In each case you will experimentally determine whether momentum is conserved and the extent to which kinetic energy is conserved.

Materials

1. Air track
2. Compressor
3. Gliders with 10cm flags
4. Magnetic bumpers
5. Pasco 550 Interface
6. Photogate and stand
7. Pin and wax bumper set
8. Plastic pipe
9. Round glider weights
10. Rubber band bumpers
11. Triple-beam balance

Introduction

When momentum is conserved in a two-object collision

\[ \vec{p}_{1i} + \vec{p}_{2i} = \vec{p}_{1f} + \vec{p}_{2f} \]  
(1)

Rearranging, we have

\[ \vec{p}_{1f} - \vec{p}_{1i} = -(\vec{p}_{2f} - \vec{p}_{2i}) \]  
(2)

or equivalently

\[ \Delta \vec{p}_1 = -\Delta \vec{p}_2 \]  
(3)

That is, when momentum is conserved the change in the momentum of one object is equal and opposite the change in momentum of the other; the total momentum change is zero. In a one-dimensional collision we often use signs to indicate direction. In such a case total momentum tends to be the difference of two numbers and momentum change tends to be the sum of two numbers. For this reason, as pointed out above, equations (2) and (3) rather than equation (1) may provide your best test of whether or not momentum is conserved in a particular collision.

The apparatus used will consist of an air track, two gliders, two photogates, and a computer equipped with a Pasco 550 Interface. The computer will monitor the times that the photogates are blocked by the air track gliders. The air track should nearly eliminate friction on the gliders, making their collisions nearly isolated.
Procedure

Preliminary Information

Place a glider on the air track and turn on the air supply. Carefully level the track so that the glider does not preferentially drift toward one end. Plug the photogates into digital Channels 1 and 2 of the 550-Interface. Place the two photogates so that they divide the air track approximately into thirds. Position them so that the plastic flag on top of the passing glider will block the photogate beams.

Open the Pasco Capstone program on your desktop. In the "Tools" windows panel on the left side of the screen, click on "Hardware Setup". Click on the yellow circle around digital channel 1 and select "One Photogate (Single Flag)". Repeat for digital channel 2. In the "Displays" window panel to your right, double click on "Table". In the first column, click on “Select Measurement” and choose “Time in Gate, Ch 1 (s)”. Choose “Speed, ch 1 (m/s)” for the second column. Repeat this step for channel 2. (Make sure that Table 1 corresponds to the photogate in Channel 1 and Table 2 corresponds to the photogate in Channel 2.) For the speeds in the tables to be correct, the length of the plastic flag on top of the glider should be 10 cm, and they should pass through the photogates perfectly perpendicularly to the beams (you should confirm this).

In the following experiments you should start the timer (click the “Record” button), then push the gliders from opposite ends of the air track toward the center. They should collide in the region between the photogates. As soon as they have passed back out of this region you should stop the timer (click “Stop”). You will need to assign directions to your speed values recorded in your tables to make them velocities (which way you will call positive and which negative). After each experiment you will place the appropriate sign to the “velocities”.

Each time that you run a new experiment the old one will be saved (as Run 1, Run 2, ...). To erase your experiment runs simply click on “Delete LastRun” at the bottom of your screen.

Caution: These experiments should take place at fairly low speeds. You will know the gliders were going too fast if you hear a metallic clatter when they collide. This sound will probably mean that the collision has caused a glider to break through the cushion of air and bang against the air track. In such a case you no longer have a nearly isolated collision. Now you’re ready to begin!

(Nearly) Elastic Collisions

Equip each of the gliders with a rubber band bumper. By means of the triple-beam balance, carefully determine the mass of each glider. It’s time to turn the microphone on to you.
One stationary glider, one mobile glider, equal masses

Position one glider between the photogates and leave it stationary. Propel the other glider toward the stationary glider such that the rubber bands reflect one another and be careful to note which glider is detected by which photogate. Compute the momentum, \( \dot{p} = m \dot{v} \), of each glider before and after the collision. Again, keep in mind that momentum is a vector, so use appropriate signs to indicate direction; you will have to assign appropriate + or − signs to your velocities. How do the momentum changes of the gliders compare? What is the total momentum before and after the collision? Was momentum conserved in the collision to within the accuracy of your measurements?

Note that a better answer to this last question may come from considering changes in momentum, as in equations (2) and (3), rather than considering total momentum before and after, as in equation (1). Because it is fairly easy to produce a collision in which the two gliders have nearly equal but opposite momenta, it is fairly common to have a total momentum that is very small compared to the momentum of either glider. In such a case a small error in the momentum of either glider can lead to an error in the total momentum on the same order of magnitude as the total momentum itself. Such an occurrence can give the false impression that momentum was not even approximately conserved. On the other hand, because of the reversal of direction, the momentum change of either glider will tend to be large and less affected by small uncertainties.

Compute the kinetic energy \( K = \frac{1}{2} m v^2 \) of each glider before and after the collision. Since kinetic energy is a scalar, only positive numbers will be involved. Was kinetic energy conserved in the collision? If not, how much energy was lost? What became of this energy?

Two mobile gliders, equal masses

This time propel both gliders such that they collide between the photogates. Was momentum conserved in the collision to within the accuracy of your measurements? Was kinetic energy conserved in the collision?

Two mobile gliders, unequal masses

Add mass to one of the gliders, using the cylindrical masses in the kit, by positioning one mass on the post on each side of the glider. Determine the new mass of the glider. Again, propel both gliders such that they collide between the photogates. Was momentum conserved in the collision to within the accuracy of your measurements? Was kinetic energy conserved in the collision?
Completely Inelastic Collisions

Replace one of the rubber band bumpers with a pin bumper, and replace the other with a wax receptacle, into which the pin will stick when the gliders collide. At moderate speeds this bumper arrangement will cause the gliders to stick together on collision. After each collision you will need to use some small object to press the wax back into the hole made by the pin. As before, start the timer and cause the gliders to collide between the photogates. Stop the timer after they have exited together through one of the gates. In this case that photogate will have three-time intervals: one for the entering glider and two approximately equal times for the two gliders that pass together through it.

One stationary glider, one mobile glider, equal masses

Position one glider between the photogates and leave it stationary. Propel the other glider toward the stationary glider such that the pin sticks into the wax without the cases “clacking”. Is momentum conserved in this type of collision? Is kinetic energy conserved? If not, how much is lost? What becomes of the lost energy?

Two mobile gliders, equal masses

This time propel both gliders such that they collide between the photogates. If you happen to produce a collision in which they are nearly at rest after collision, analyze it for momentum and energy conservation by using zero for the final velocity; then repeat the experiment with different initial velocities which cause the gliders to come through a photogate soon after colliding. Is momentum conserved in this type of collision? Is kinetic energy conserved? If not, how much is lost? What becomes of the lost energy?